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# REACTION-DIFFUSION STEREO ALGORITHM WITH ANISOTROPIC INHIBITORY DIFFUSION

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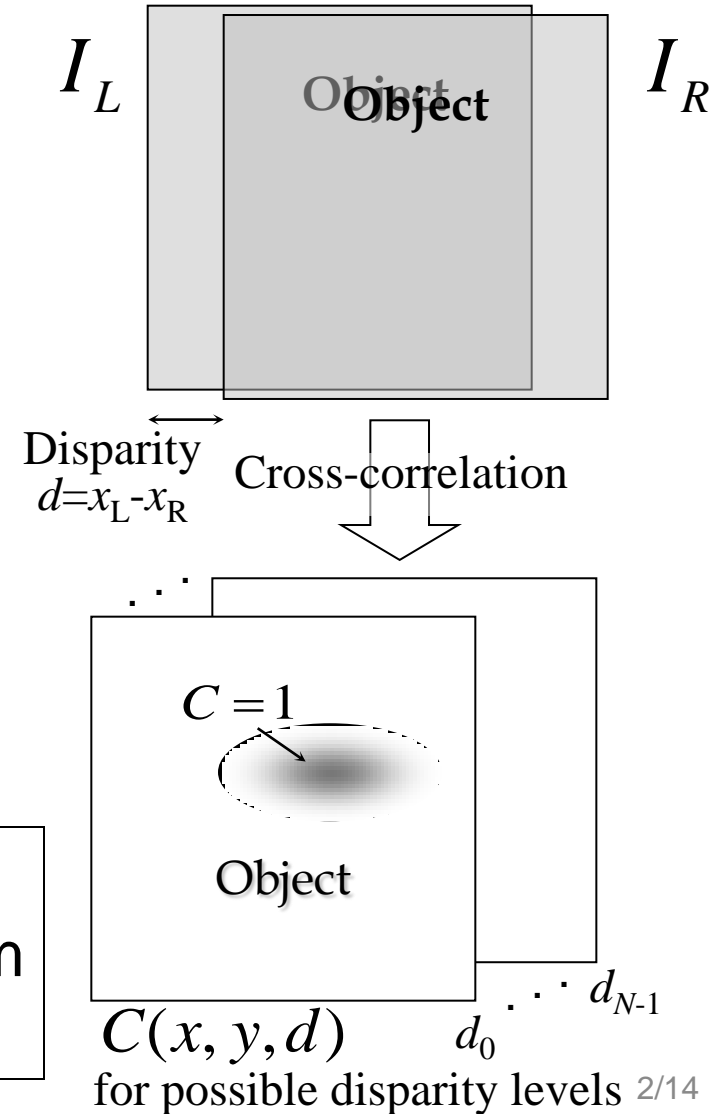
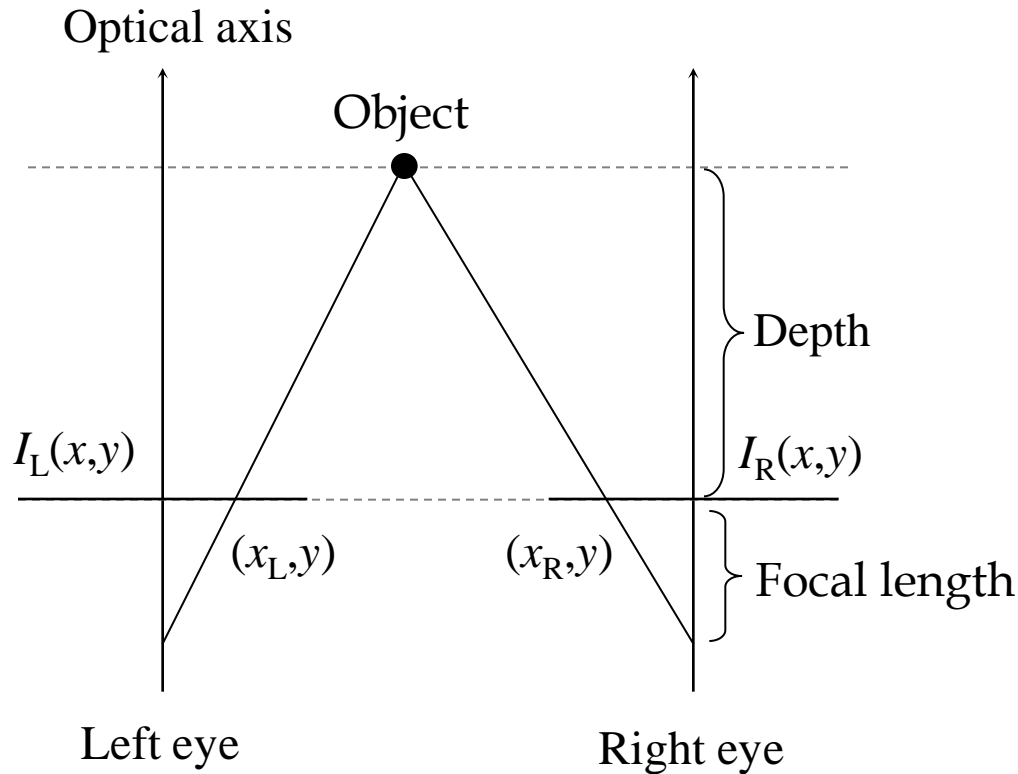
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# Introduction: Binocular Stereo Vision



Stereo correspondence problem  
 $\Rightarrow$  Segmentation problem  
**Depth discontinuity** areas cause error.

# Previous Stereo Algorithms

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- Marr & Poggio, *Proc. Roy. Soc. Lond.*, 1979
  - original cooperative algorithm
  - continuity & uniqueness constraints
  - bio-inspired algorithm
- Zitnick & Kanade, *IEEE-PAMI*, 2000
  - modern cooperative algorithm + occlusion detection
- Sun et al., *IEEE-PAMI*, 2003
  - belief-propagation algorithm
- Deng et al., *IEEE-PAMI*, 2007
  - graph-cuts algorithm

# Diffusion Equation & PDE Approach in Image Processing & Computer Vision Research

- Koenderink, *Biol. Cybern.*, 1984
  - Diffusion equation = Gaussian filter
- Perona & Malik, *IEEE-PAMI*, 1990
- Black et al., *IEEE-IP*, 1998
  - Anisotropic diffusion
- Mrázek & Navara, *IJCV*, 2003
  - Stopping time for non-linear diffusion filtering

Isotropic diffusion equation:

$$\partial_t u = D \nabla^2 u + s$$

$D$ : diffusion coefficient,  $s$ : source

=> uniform distribution

Anisotropic diffusion equation:

$$\partial_t u = \nabla \cdot [D(x, y) \nabla u] + s$$

$D(x, y)$ : anisotropic diffusion coefficient

diffusion depends on a position  $(x, y)$

$\partial_t = \partial / \partial t$ ,  $\nabla^2$ : Laplacian Operator

# Reaction-Diffusion Algorithm

- Adamatzky et al., *Reaction-Diffusion Computers*, 2005
  - proposed novel computer architecture, by utilizing reaction-diffusion equations.
  - natural computing.
- FitzHugh-Nagumo reaction-diffusion equations

$$\partial_t u = D_u \nabla^2 u + \frac{1}{\varepsilon} [u(u - a)(1 - u) - v]$$

Constants:  
 $0 < \varepsilon \ll 1$   
 $a, b$

$$\partial_t v = \underbrace{D_v \nabla^2 v}_{\text{Diffusion}} + \underbrace{u - bv}_{\text{Reaction}}$$

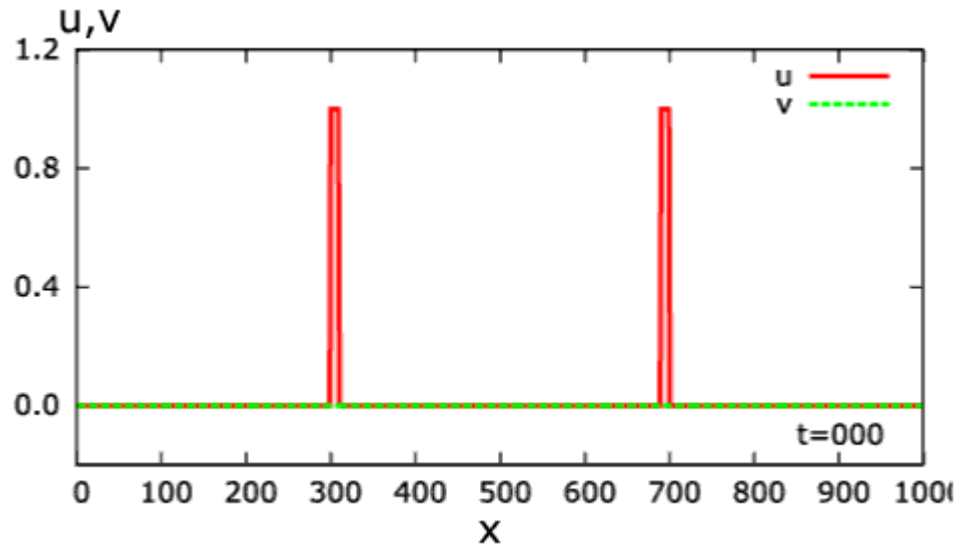
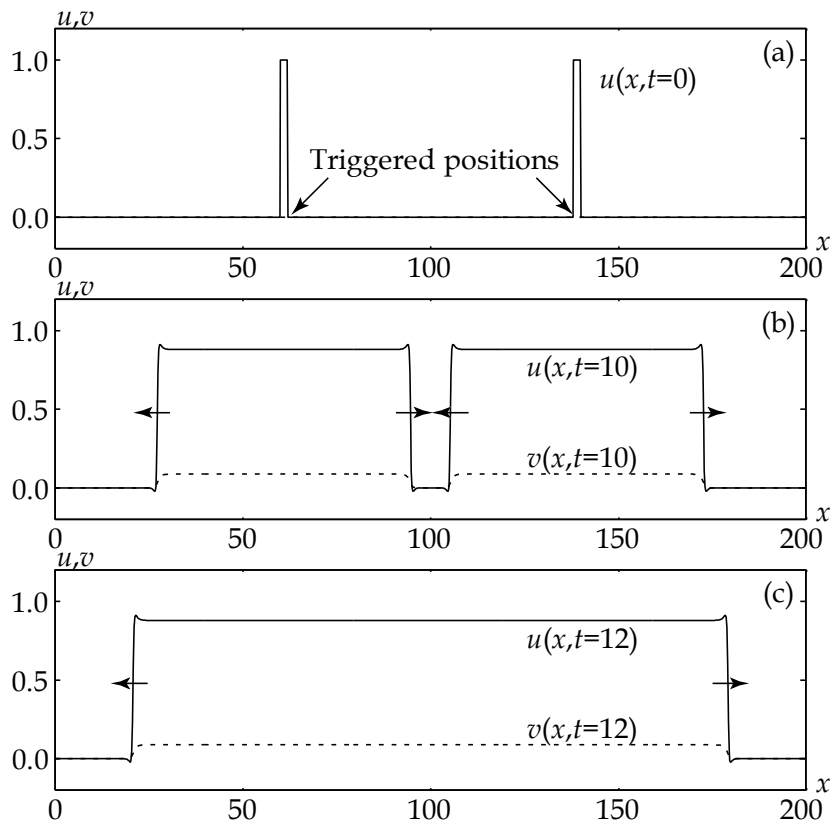
$u$ : activator,  $v$ : inhibitor

FitzHugh, *Biophysical J.*, 1961

Nagumo et al., *Proc. IRE*, 1962 5/14

# Reaction-Diffusion Equations in 1D Space

- FitzHugh-Nagumo equations: bi-stable system



Parameter settings:

$$D_u=1.0, D_v=3.0$$

$$a=0.05, b=10.0, \varepsilon=1/100$$

# Reaction-Diffusion Stereo Algorithm

- Nomura et al., *Machine Vision and Applications* (2009)

$$\partial_t u_n(x, y, t) = D_u \nabla^2 u_n + f(u_n, v_n, u_{\max}) + \mu C(x, y, d_n)$$

$$\partial_t v_n(x, y, t) = D_v \nabla^2 v_n + g(u_n, v_n)$$

The diffusion term  $D_u \nabla^2 u_n$  drives the propagation of region of the disparity level  $d_n$ .

$$f(u_n, v_n, u_{\max}) = \frac{1}{\varepsilon} \left[ u_n (u_n - a(u_{\max})) (1 - u_n) - v_n \right]$$

$$g(u_n, v_n) = u_n - b v_n$$

Disparity map:

$$M(x, y, t) = \operatorname{argmax}_{n \in \{0, 1, \dots, N-1\}} u_n(x, y, t)$$

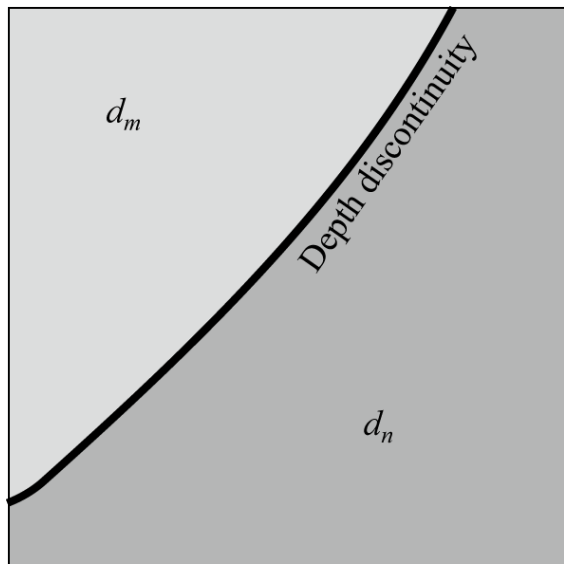
$\mu$ : constant  
 $N$ : total number of possible disparity levels  
 $C$ : similarity measure  
 $d_n$ : disparity level

# Proposed Reaction-Diffusion Stereo Algorithm

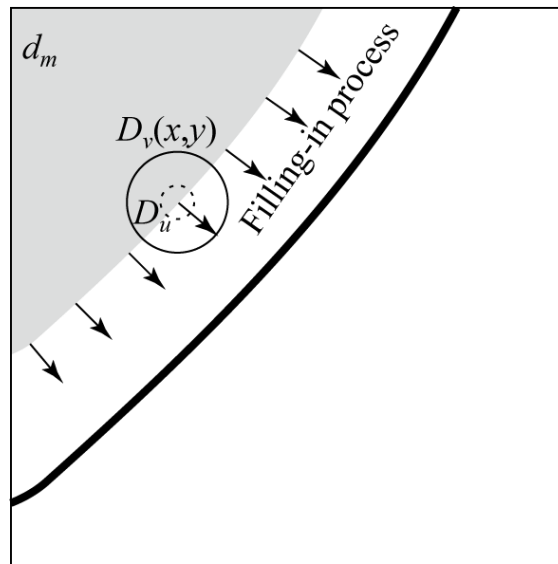
$$\partial_t u_n = D_u \nabla^2 u_n + f(u_n, v_n, u_{\max}) + \mu C(x, y, d_n)$$

$$\partial_t v_n = \nabla \cdot \left[ \underline{D_v(x, y)} \nabla v_n \right] + g(u_n, v_n)$$

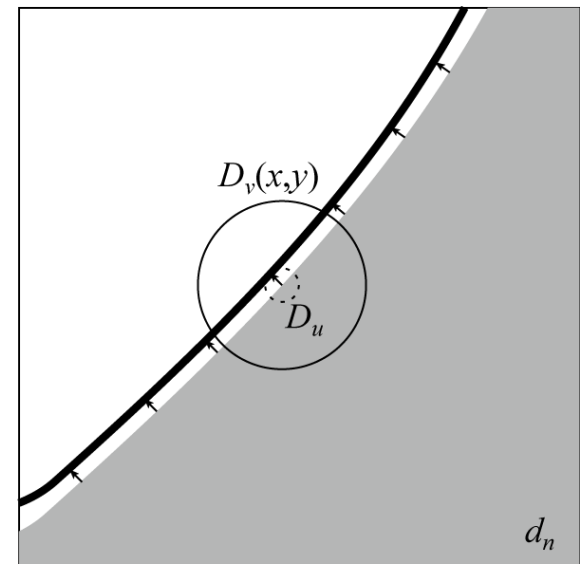
The diffusion coefficient  $D_v(x, y)$  is set to be **large** around **depth-discontinuity** areas.



(a) Stereo disparity map



(b)  $m$ -th reaction-diffusion system



(c)  $n$ -th reaction-diffusion system



# How to Estimate the Inhibitory Diffusion Coefficient $D_v(x,y)$

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Initial disparity map

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Edges detected from intensity image

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Edge detection algorithm with reaction-diffusion equations:

- Nomura et al., *J. Phys. Soc. Jpn.*, 2003
  - Edge detection & Segmentation
  - Discrete version of reaction-diffusion equations
  - Thresholding
- Nomura et al., *Patt. Recog. Image Anal.*, 2008
  - Edge detection utilizing reaction-diffusion equations
  - Adaptive threshold level

## Proposed Reaction-Diffusion Stereo Algorithm (cont.)

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- Step 1: Compute cross-correlation functions.
- Step 2: Detect edges in the left image.
- Step 3: Estimate  $D_v(x,y)$  with an initial disparity map and an edge map.
- Step 4: Compute reaction-diffusion equations iteratively.
- Step 5: Estimate a disparity map.

# Experimental Results

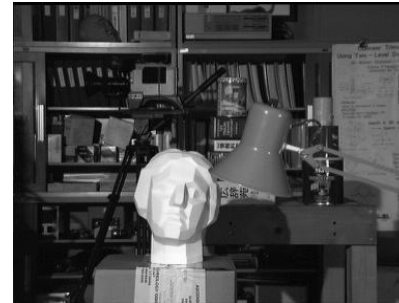
- The Middlebury stereo vision page provides
  - stereo image pairs,
  - ground-truth data of disparity maps,
  - definition of areas (occlusion area & depth discontinuity),
  - scores of other stereo algorithms
  - <http://vision.middlebury.edu/stereo/>
- Example of stereo image pairs



**CONES** 450X375 pixels  
60 disparity levels



**TEDDY** 450X375 pixels  
60 disparity levels



**TSUKUBA**  
384X288 pixels  
15 disparity levels



**VENUS** 434X383 pixels  
30 disparity levels

# Results on the Middlebury Stereo Data

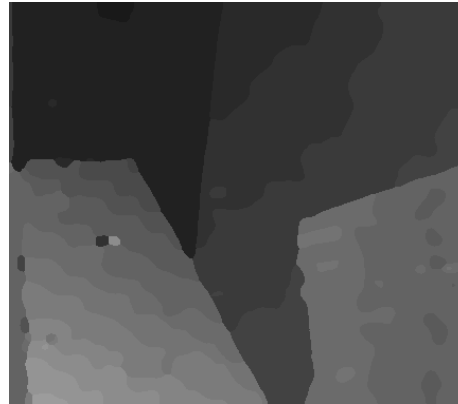
Algorithm		Reaction-diffusion stereo algorithm						Adapting BP (Klaus et al., <i>Proc. ICPR</i> , 2006)
version		Original (Nomura et al., <i>Mach. Vis. Appl.</i> , 2009)		IIEI (Nomura et al., <i>Proc. VISAPP</i> , 2009)		Proposed		
Image pair	Area	BMP (%)	RMS (pixel)	BMP (%)	RMS (pixel)	BMP (%)	RMS (pixel)	BMP (%)
TSUKUBA	nonocc.	<u>6.77</u>	<u>1.42</u>	8.51	1.54	7.02	1.47	1.11
	all	<u>8.53</u>	<u>1.61</u>	10.23	1.72	8.54	1.64	1.37
	disc.	18.68	<u>2.47</u>	19.42	2.52	<u>18.55</u>	2.60	5.79
VENUS	nonocc.	2.81	0.75	3.17	0.77	<u>1.21</u>	<u>0.59</u>	0.10
	all	3.97	0.92	4.33	0.92	<u>2.44</u>	<u>0.80</u>	0.21
	<b>disc.</b>	<b>21.64</b>	<b>2.01</b>	<b>19.62</b>	<b>1.88</b>	<b><u>8.12</u></b>	<b><u>1.52</u></b>	1.44
TEDDY	nonocc.	14.26	<u>2.19</u>	<u>14.00</u>	2.38	14.56	2.29	4.22
	all	20.26	<u>3.23</u>	<u>20.00</u>	4.36	20.64	3.32	7.06
	disc.	29.19	<u>3.36</u>	28.89	3.48	<u>27.98</u>	3.45	11.8
CONES	nonocc.	<u>5.03</u>	1.94	5.08	<u>1.85</u>	5.21	1.88	2.48
	all	<u>12.13</u>	<u>3.08</u>	12.35	5.45	13.34	3.15	7.92
	disc.	14.06	3.34	<u>13.67</u>	<u>3.03</u>	14.08	3.17	7.32

nonocc.: non-occlusion area, all: all area, disc.: depth discontinuity area  
 BMP: bad-match-percentage, RMS: Root Mean Squares

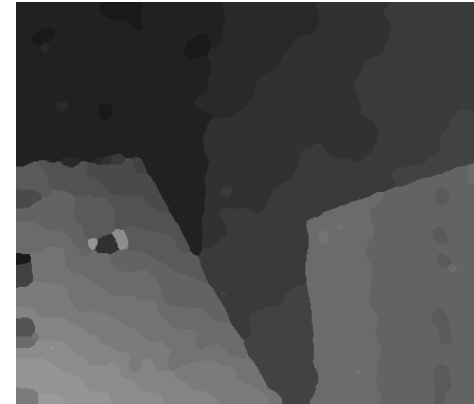
# Example: VENUS



Left image



Disparity map  
(Proposed)



Disparity map  
(Original)

$M$  (pixel)

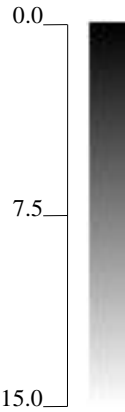
0

15

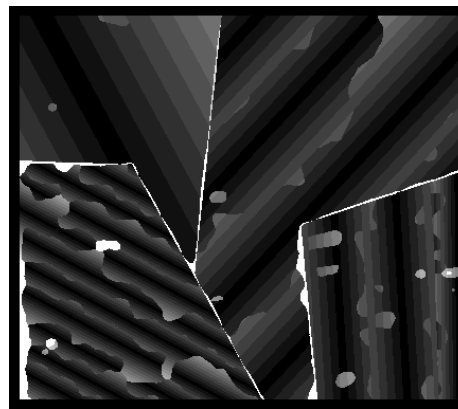
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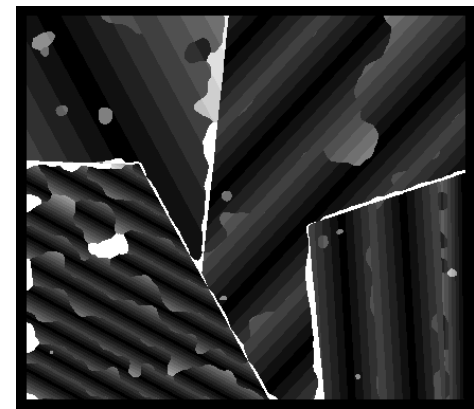
$D_v$



$D_v$



Error distribution  
(Proposed)



Error distribution  
(Original)

$E$  (pixel)

0.0

1.0

2.0



# Conclusion & Future Work

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- Conclusion:
  - We proposed integration of intensity edge information into the reaction-diffusion stereo algorithm.
  - Key point: inhibitory diffusion coefficient is set to be large around depth discontinuity areas.
  - We confirmed performance of the proposed algorithm.
- Future work:
  - How to estimate depth discontinuity areas.
  - Dynamic interactions between disparity detection and edge detection.

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